

Aeration 2

$$\frac{dC}{dt} = K_L(C^* - C) - xQ$$

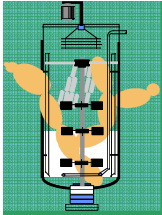
On what and how saturation oxygen concentration C^* depends ? ✓

On what and how ... K_L ?

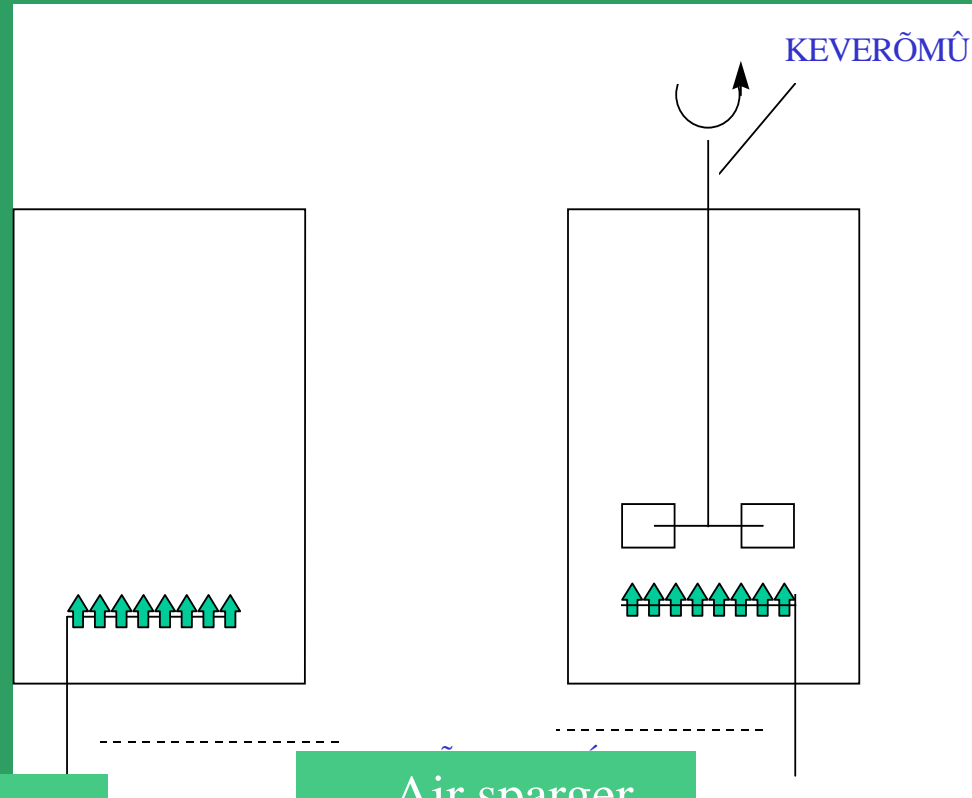
On what and how... a ?

On what and how $K_L a$?

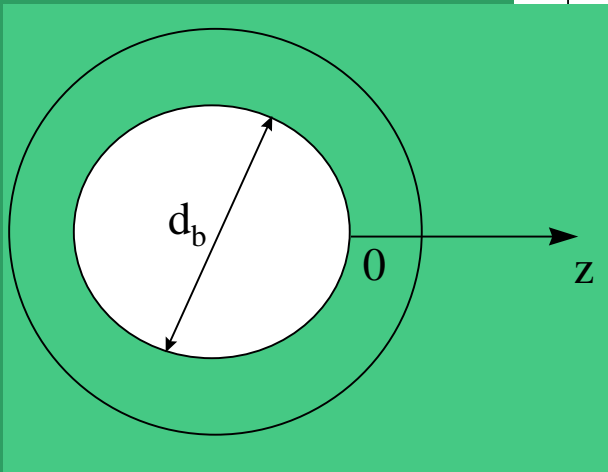
Aeration 3



Not mixed reactors
Only aeration



Air sparger

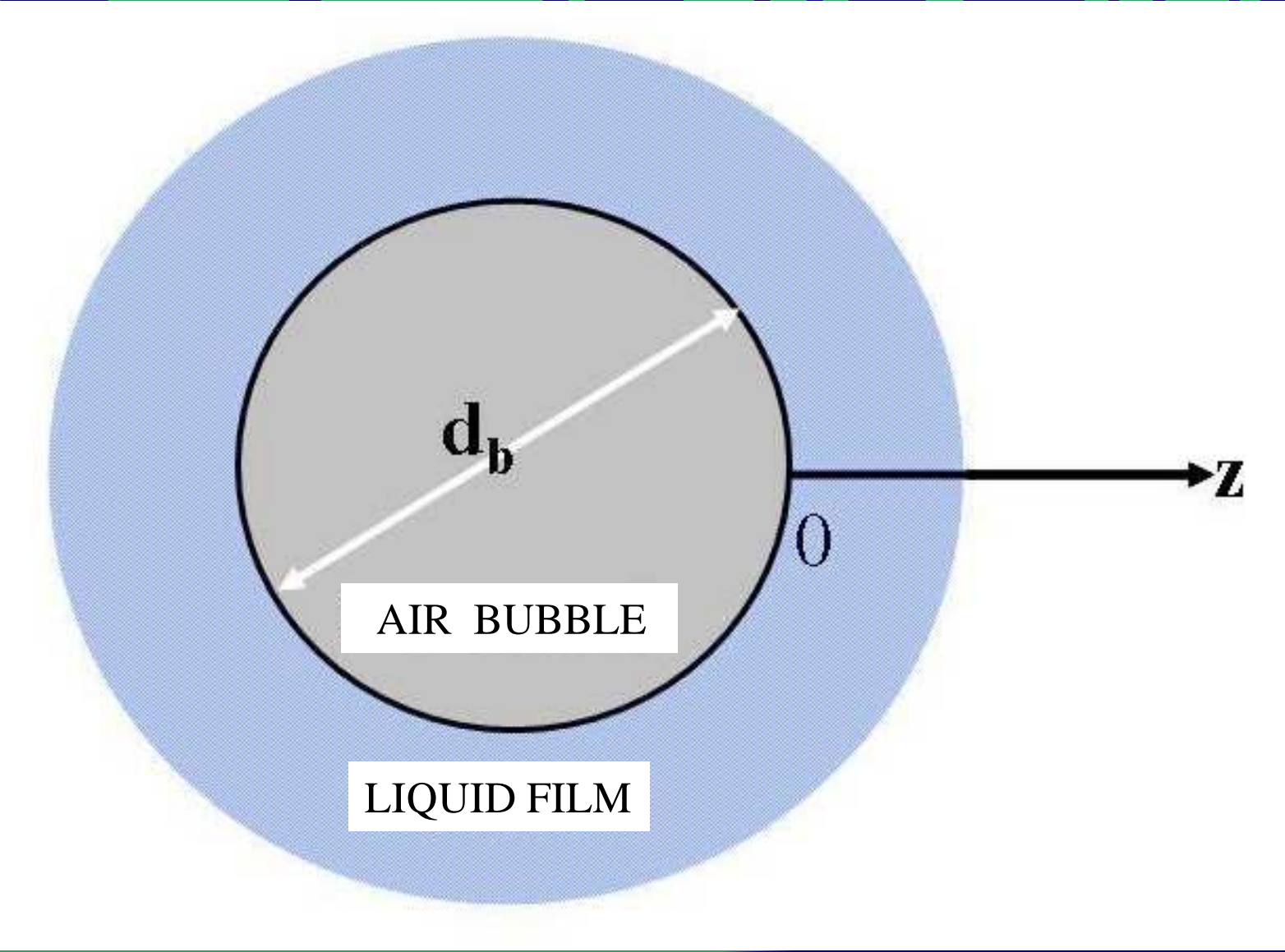


$$\frac{dC}{dt} = -D_{O_2} \left(\frac{\partial C}{\partial z} \right)_{z=0}$$

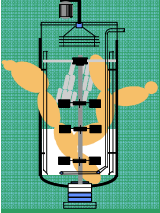
Fick-law of diffusion

$$dC/dt = k_L (C^* - C).$$

Oxygen flux through unit surface area



Aeration 3



Dimensionless form

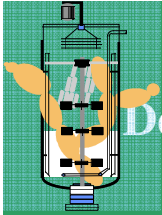
$$\bar{C} = f(\bar{z}, Sh, Sc, Gr)$$

$$Sh = g(Sc, Gr)$$

**Dimensionless mass
transfer coefficient:
Sherwood-number**

There are numerous correlations describing K_1 (Sh) as a function of hydrodynamic Behaviour and liquid characteristics

Aeration 3



Definition, explanation

general form

form used for oxygen m.tr.

REYNOLDS No

$$Re = \frac{\text{inertial forces}}{\text{viscous forces}} \quad \frac{dv\rho}{\mu} \quad \frac{d_b v_b \rho_l}{\mu_l}$$

PECLET No

$$Pe = \frac{\text{konvective component stream}}{\text{konduktive component stream}} \quad \frac{dv}{D} \quad \frac{d_b v_b}{D_{O_2}}$$

SCHMIDT No

$$Sc = \frac{\text{momentum diffusivity}}{\text{mass diffusivity}} \quad \frac{\mu}{\rho D} \quad \frac{\mu_l}{\rho_l D_{O_2}}$$

FROUDE No

$$Fr = \frac{\text{centrifugal force}}{\text{gravitational force}} \quad \frac{v^2}{gL} \quad -$$

GRASHOF No

(Archimédes-No)

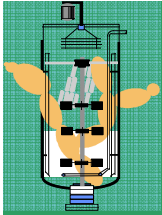
$$Gr = \frac{\text{buoyant force}}{\text{viscous force}} \quad \frac{d^3 \rho g \Delta \rho}{\mu^2} \quad \frac{d_b^3 \rho_l g (\rho_l - \rho_g)}{\mu_l^2}$$

SHERWOOD No

(dimensionless

Mass tr. coeff.)

$$Sh = \frac{\text{bubble diameter}}{\text{film thickness}} \quad \frac{kd}{D} \quad \frac{k_l d_b}{D_{O_2}}$$



Aeration 3

Example for estimating k_1

2. **CALDERBANK and MOO-YOUNG** in most lab and industrial aerated reactors bubbles move up and/or down in groups, clusters, they are in interaction with each other (influence each other's movement) ((single, independently moving bubbles are rare in real situations))

$$d_b < 2,5 \text{ mm}$$

$$\text{Sh} = \frac{k_L d_b}{D_{O_2}} = 0,31 \text{Gr}^{\frac{1}{3}} \text{Sc}^{\frac{1}{3}}$$

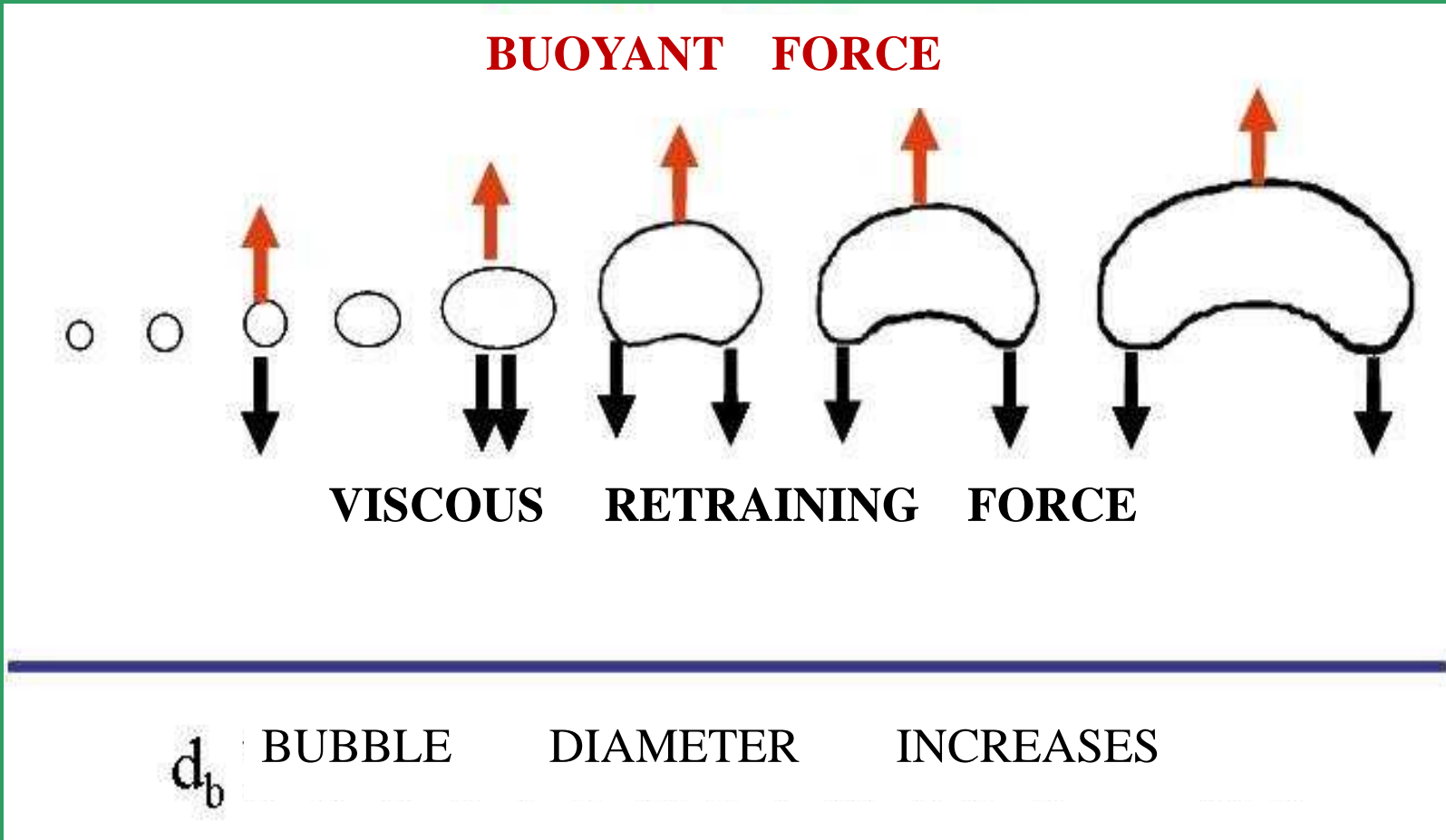
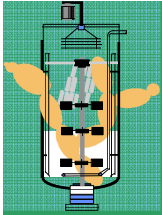
hidrofil materials
Small holes
(sintered plates, bubble columns)

$$d_b > 2,5 \text{ mm}$$

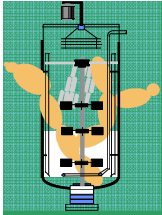
$$\text{Sh} = \frac{k_L d_b}{D_{O_2}} = 0,42 \text{Gr}^{\frac{1}{3}} \text{Sc}^{\frac{1}{2}}$$

Pure water
Sieve tray

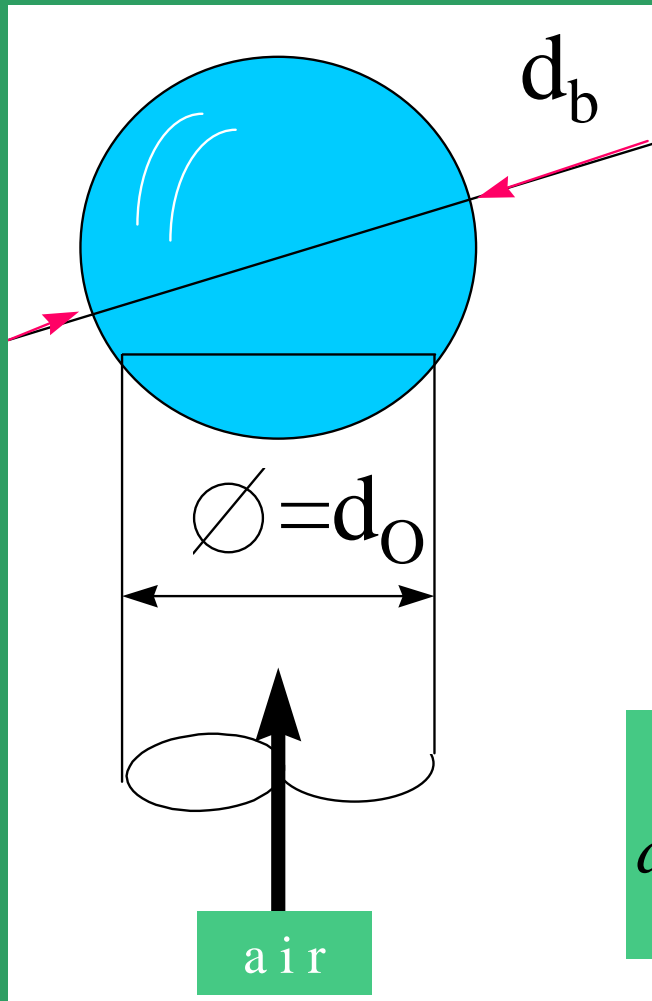
Aeration 3



Aeration 3



ESTIMATION OF a



At birth of a bubble there is an equilibrium between buoyant force and restraining force (surface tension on the circumference of the hole).

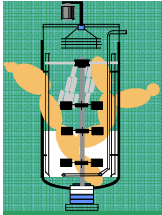
$$\frac{d_b^3 \pi \Delta \rho g}{6} = \pi d_o \sigma$$

σ surface tension

$$d_b = \left(\frac{6 \sigma d_o}{g \Delta \rho} \right)^{\frac{1}{3}} \quad f_{\text{one bubble}} = \pi d_b^2$$

How many bubbles are present in the system at a given time?

Aeration 3



How many bubbles are present in the system at a given time?

It depends on residence time.

$$t_b = \frac{H_L}{v_b}$$

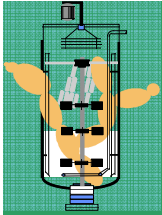
H_L - liquid heights

v_b - bubble velocity.

v_b is not constant, it varies while moves upward from the hole to the surface.

Bubble velocity: usually terminal v. at the surface (when explodes into the gas phase above.

Aeration 3



$$a = \frac{1}{V} nqt_b \frac{\pi d_b^2}{\pi d_b^3} = \frac{nqt_b}{V} \frac{6}{d_b}$$

Total bubble volume
In the reactor
 Surface of one bubble
 Volume of one bubble

Specific surface of one bubble

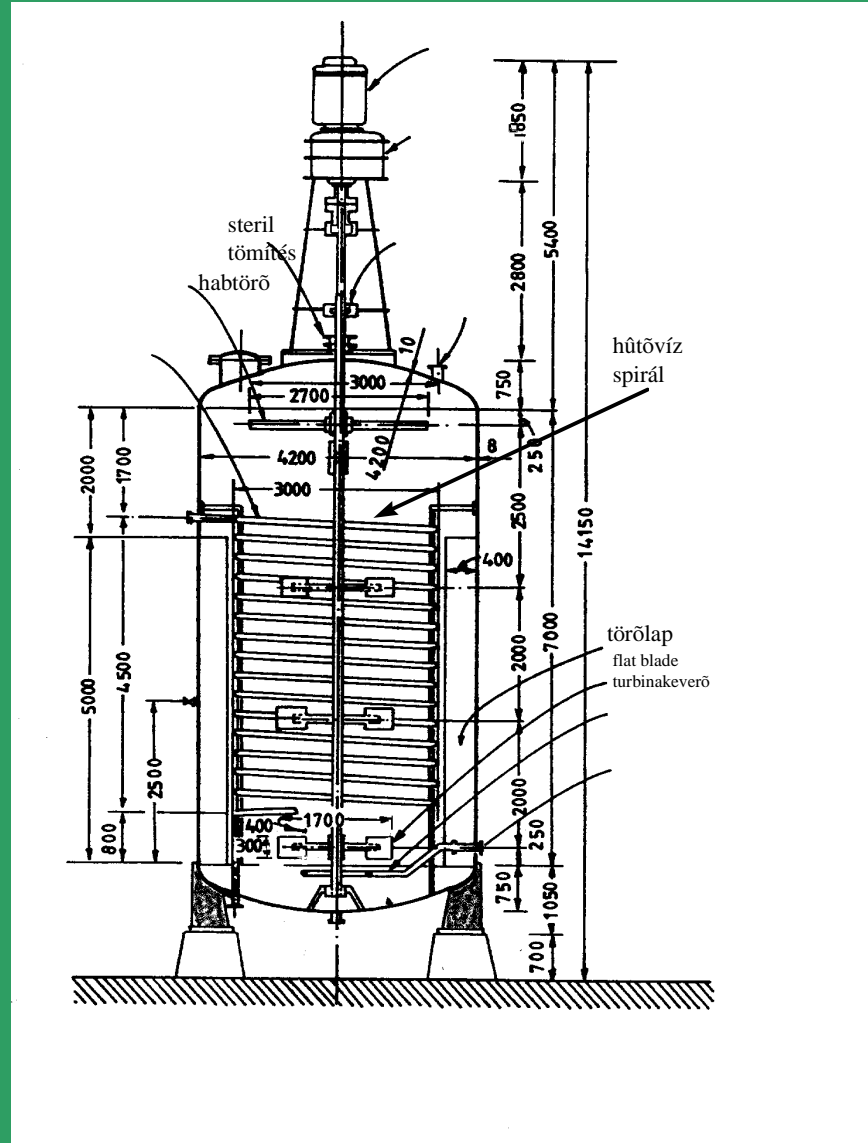
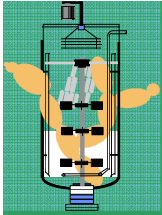
$$a = H_0 \frac{6}{d_b}$$

Hold up = $\frac{\text{GAS VOLUME}}{\text{TOTAL VOLUME}}$

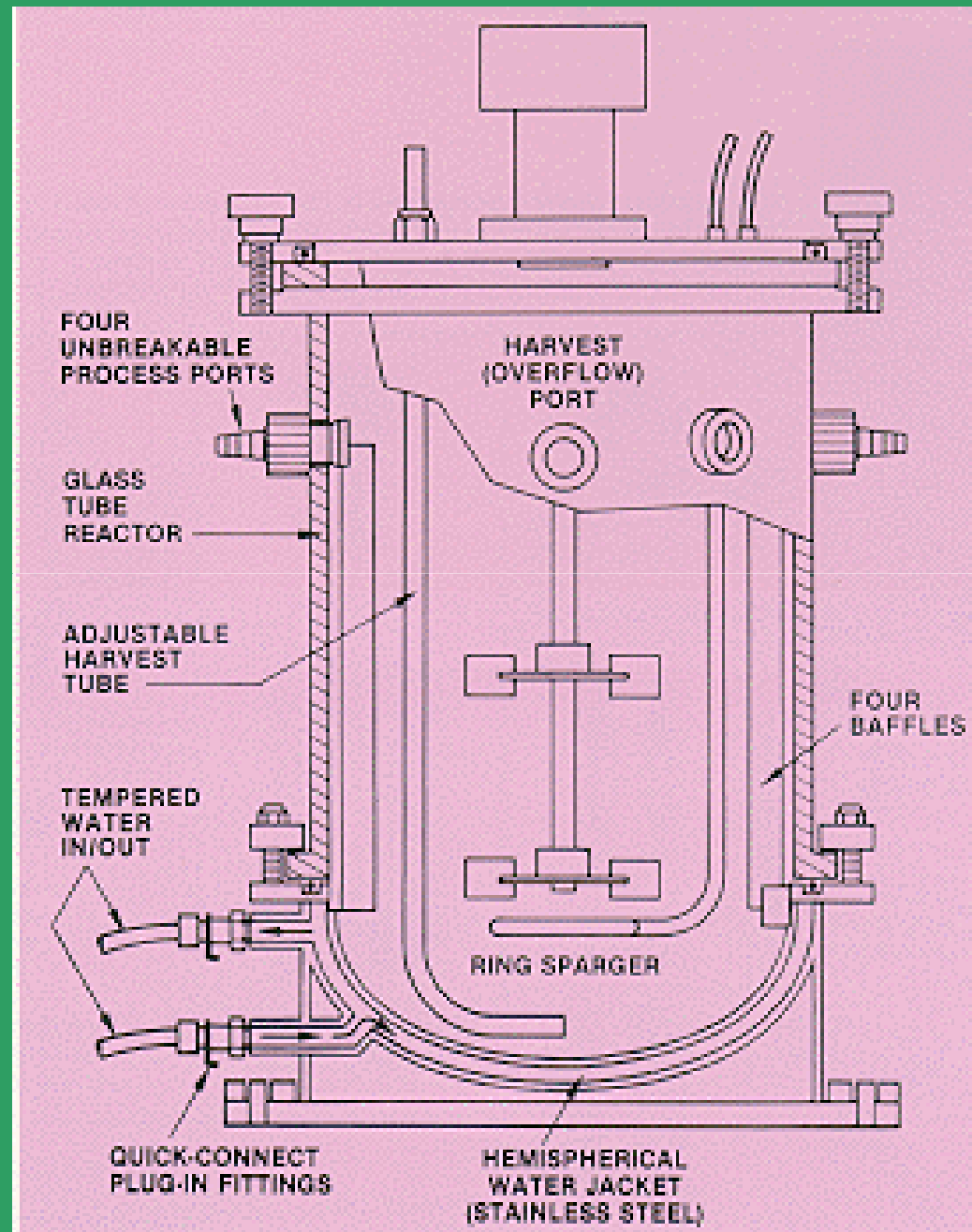
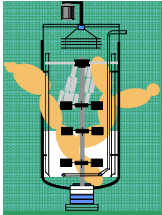
HOW CAN WE INCREASE?

Aeration 3

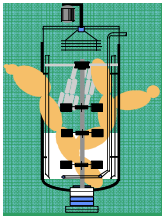
OXYGEN MASS TRANSFER IN MIXED REACTOR



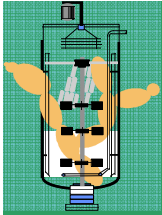
Aeration 3



Aeration 3



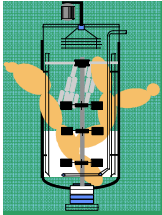
Aeration 3



MSG, JAPAN
HOFU



63420 GALLON
100 FEET



Aeration 3

ROLE OF MIXING:

-Energy input to the liquid

moving
heat

P/V  $K_L a$

-Dispersion of bubbling gas in the liquid

BUBBLE FORMATION, MASS TRANSFER

-Separation of gas from liquid

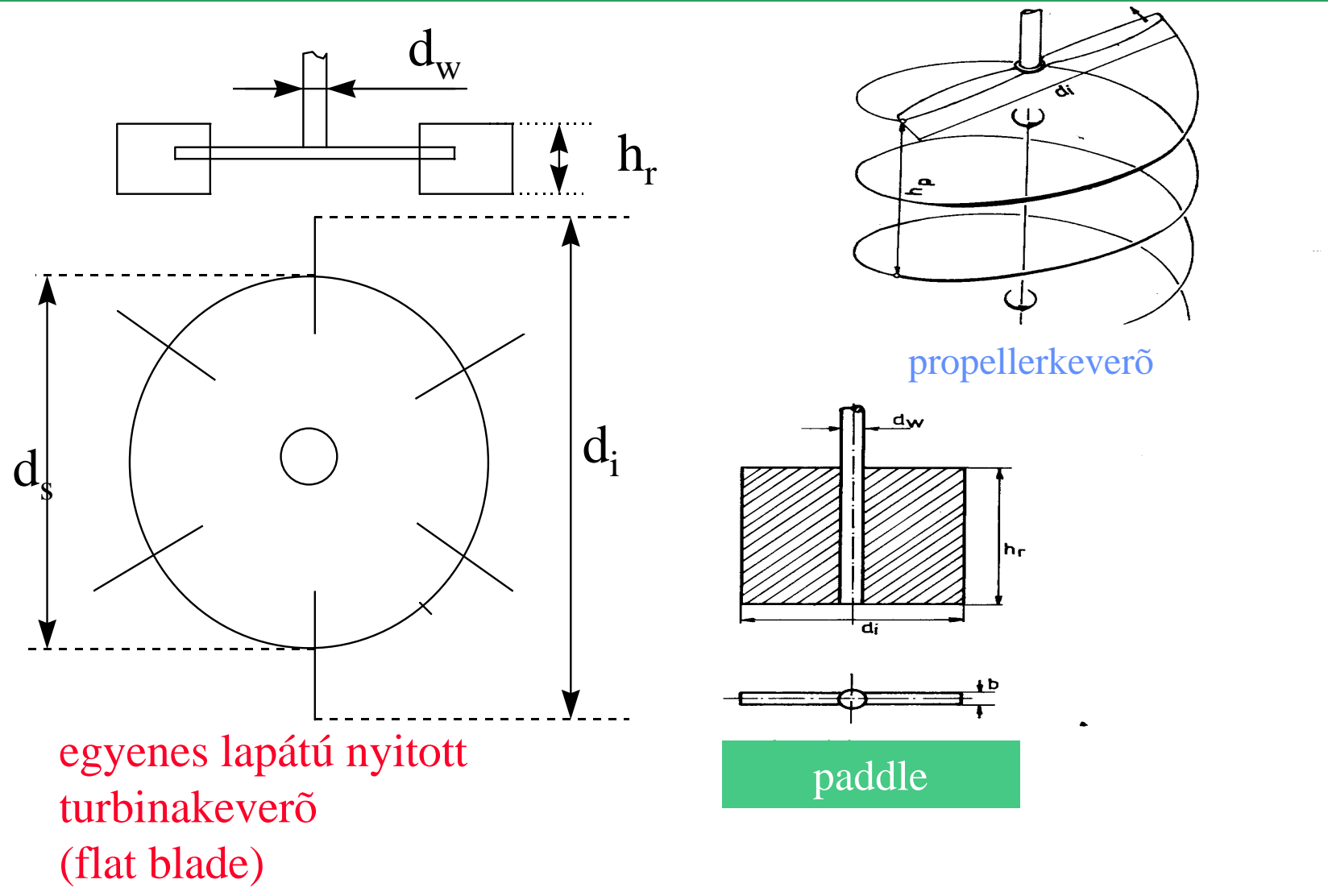
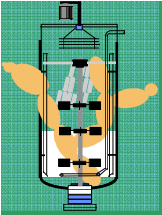
REVERSE MASS TRANSFER CO_2

-good mixing of the dissolved and suspended materials in the liquid

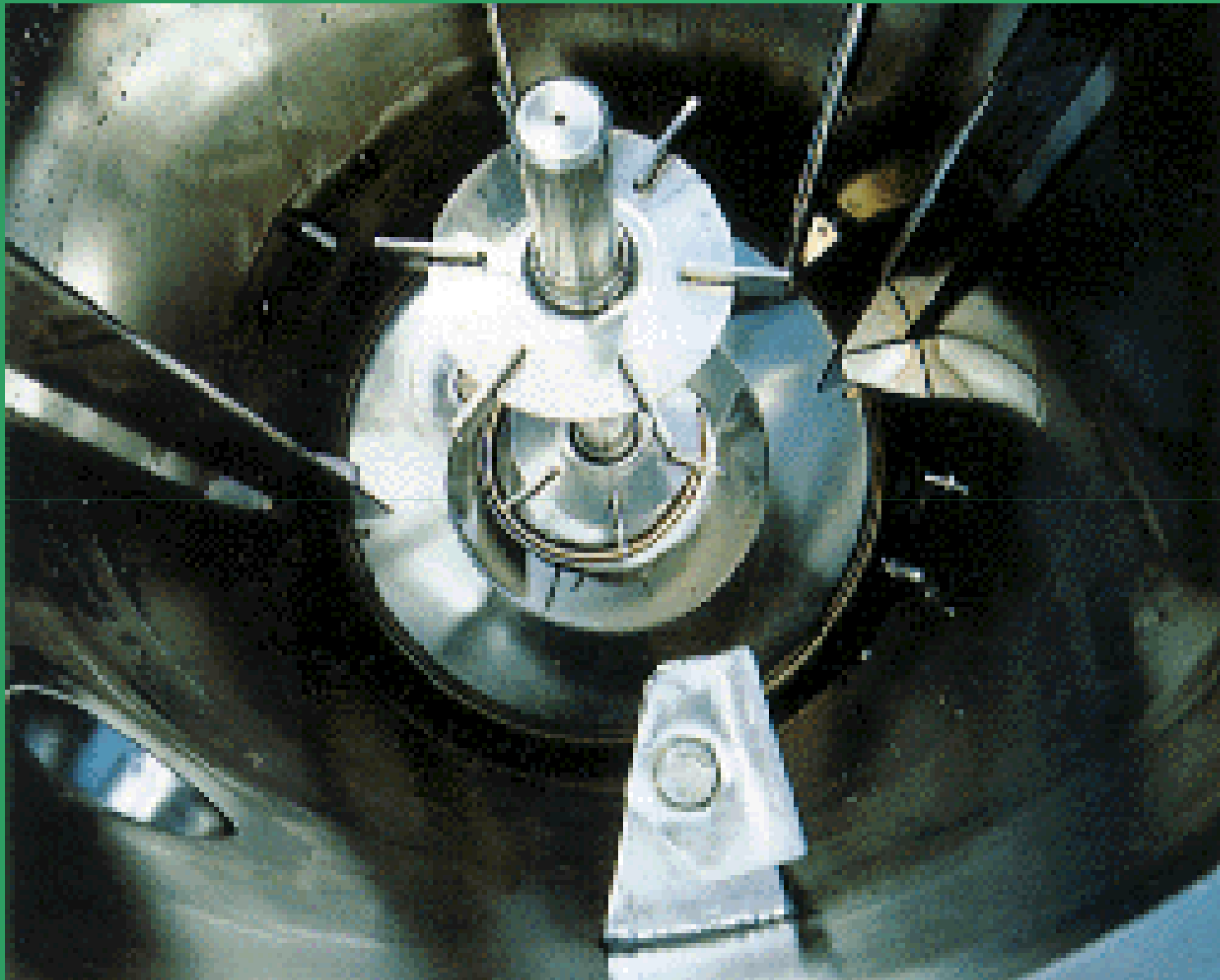
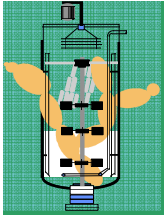
GENERAL MIXING FUNCTION

substrates, products...

Aeration 3



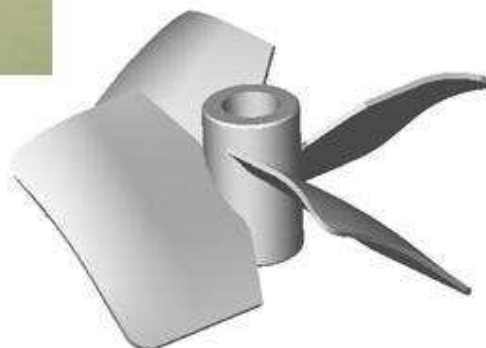
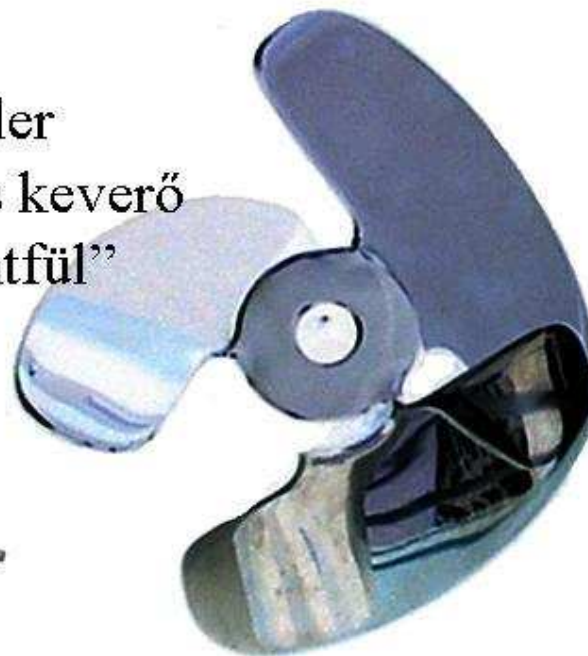
Aeration 3



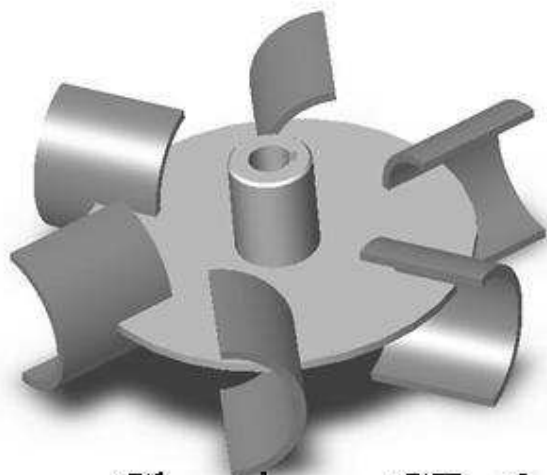


Rushton-turbina

Propeller
axiális keverő
„elefántfül”



Maxflo és Lightning
axiális keverők

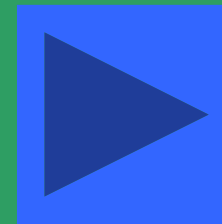
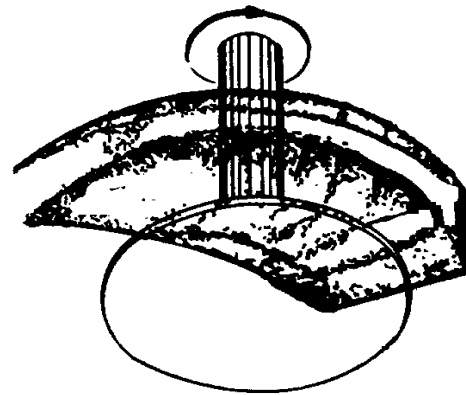
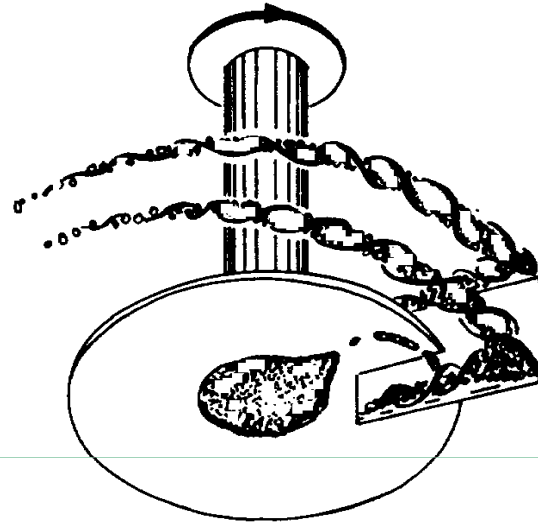
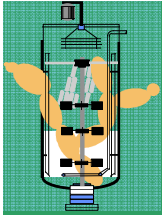


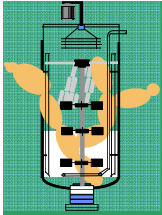
Chemineer CD-6



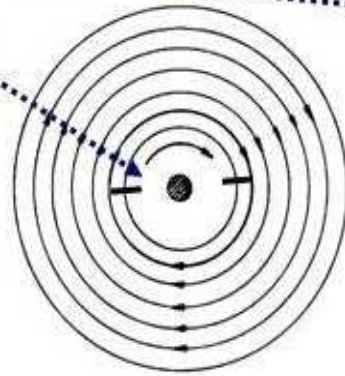
Chemineer BT-6

Aeration 3

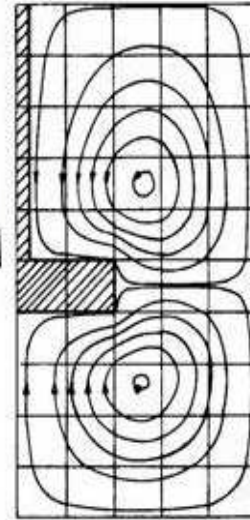




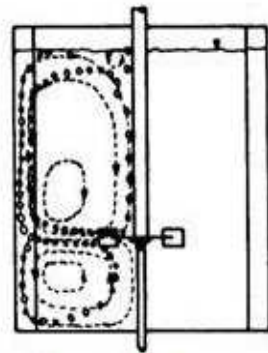
agitator



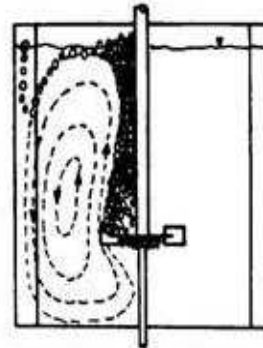
primary
liquid stream



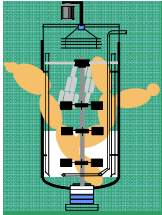
secondary
liquid stream



Bubble motion
at small gas velocity
good g/f dispersion



Bubble motion
at large gas velocity
flooding



Aeration 3

Power uptake of the mixing device

$$P = AD_i^5 N^3 \rho \text{Re}^m \text{Fr}^n \left(\frac{W_i}{D_i} \right)^\alpha \left(\frac{D_T}{D_i} \right)^\beta \left(\frac{H_L}{D_i} \right)^\gamma \dots$$

mixing Re

$$\text{Re} = \frac{D_i \cdot N D_i \rho}{\mu} = \frac{N D_i^2 \rho}{\mu} \quad \left(\text{ált.: } \text{Re} = \frac{dv\rho}{\mu} \right)$$

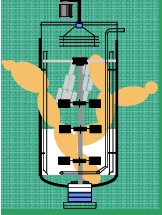
$ND\pi = \text{kerületi sebesség}$

ρ - specific density
 N - revolution rate of mixer.

Mixing Fr

$$\text{Fr} = \frac{(D_i N)^2}{g D_i} = \frac{D_i N^2}{g} \quad \left(\text{see.: } \text{Fr} = \frac{v^2}{gL} \right)$$

Aeration 3

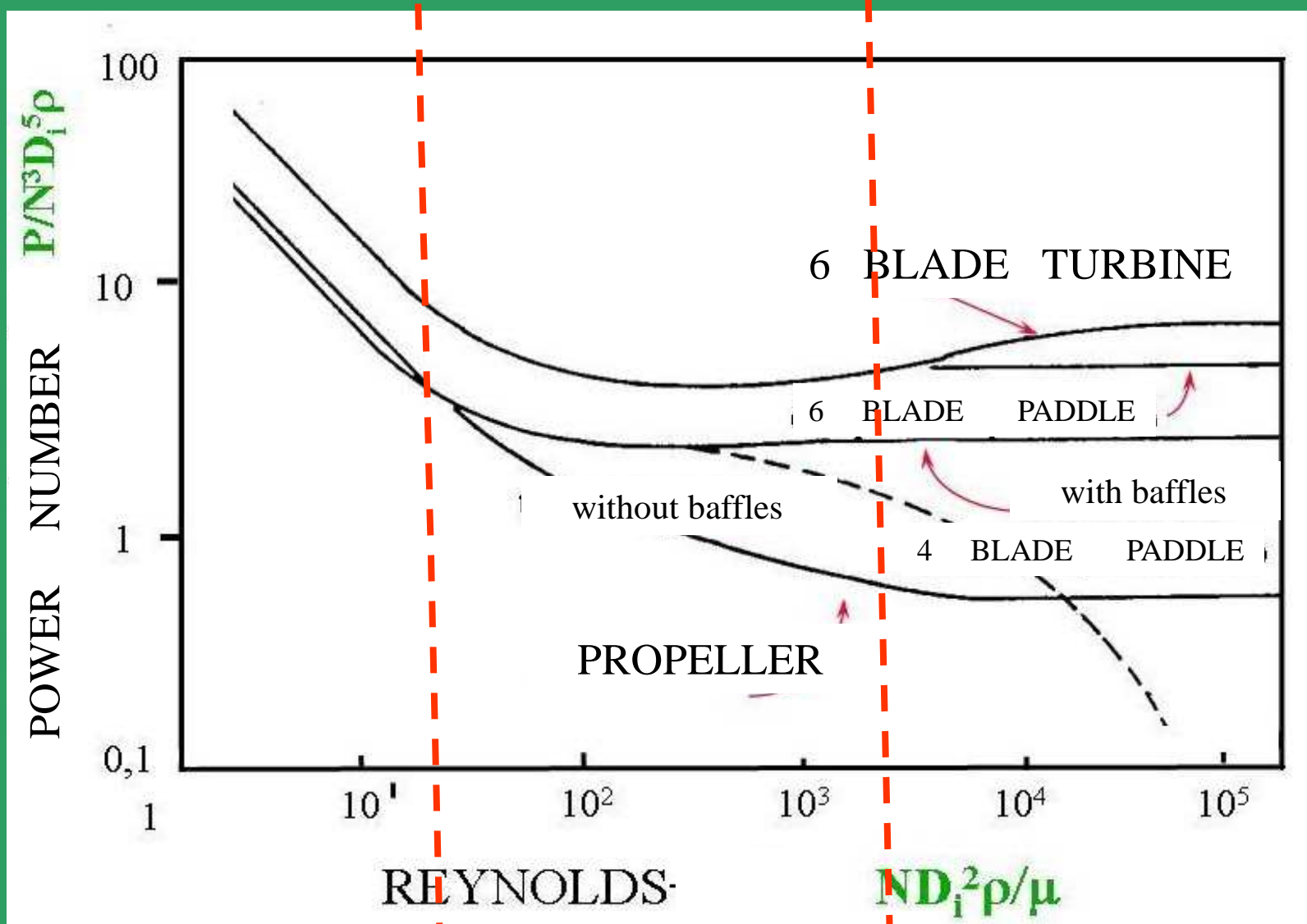


For a bioreactor of a given geometry

$$P = A' D_i^5 N^3 \rho \text{Re}^m \text{Fr}^n$$

Power number (Ne=Newton-szám vagy Eu=Euler-szám) :

$$N_P = \frac{P}{D_i^5 N^3 \rho} = A' \text{Re}^m \text{Fr}^n$$



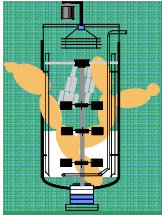
$$N_p = A' Re^{-1}$$

$$P = A' \mu D_i^3 N^2$$

$$N_p = A'$$

$$P = A' D_i^5 N^3 \rho$$

Aeration 3

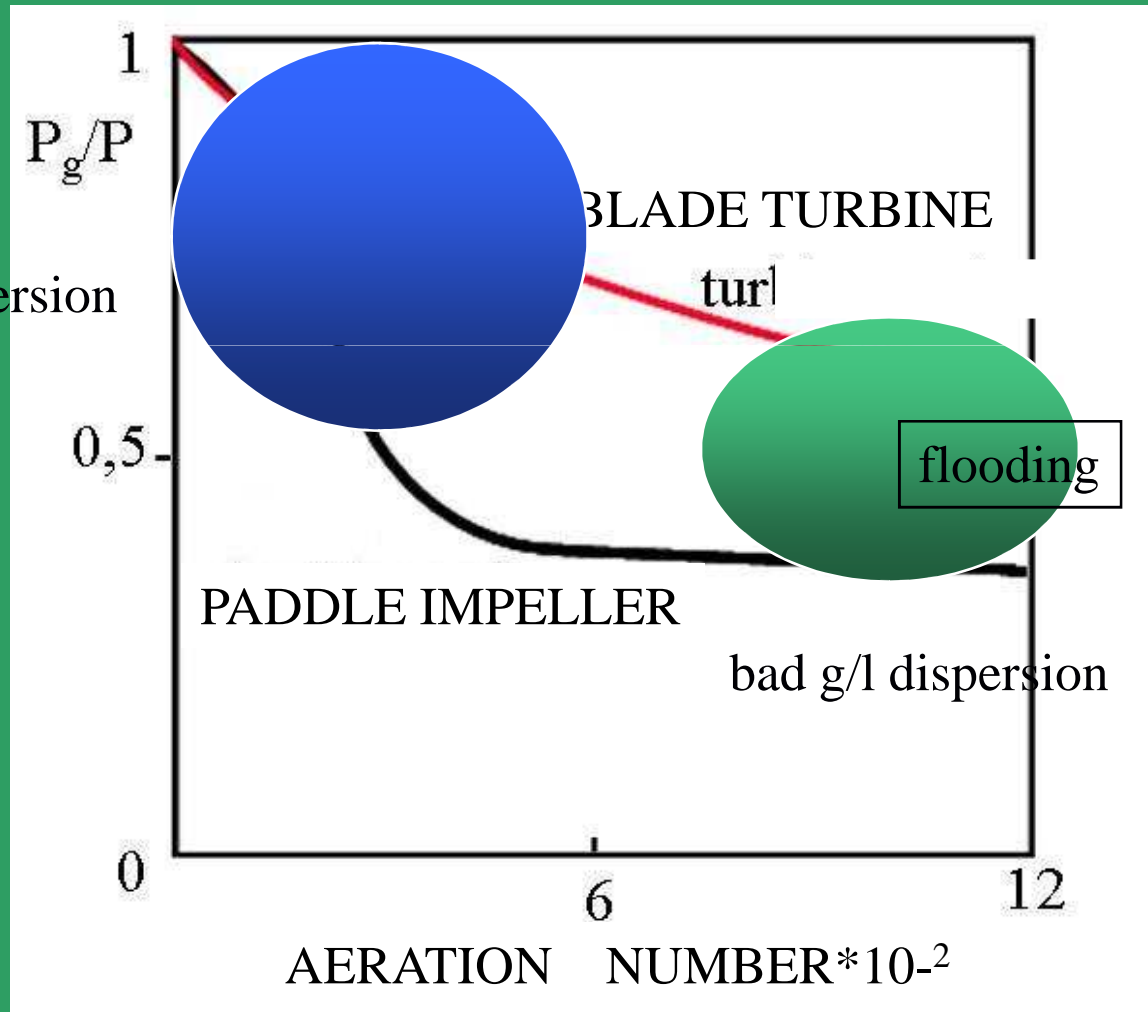


P decrease when aerating

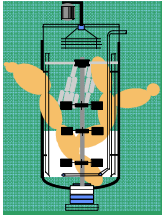
$$\frac{P_g}{P} = f(Na)$$

$$Na = \frac{\text{apparent superficial aeration rate}}{\text{keverő kerületi sebessége}} = \frac{\frac{F \text{ m}^3 / \text{s}}{D_i^2 \pi \text{ m}^2}}{ND_i \pi \text{ m} / \text{s}} = \frac{F}{ND_i^3}$$

good g/l dispersion



0,25-0,4



Aeration 3

$$K_L a \propto \left(\frac{P_g}{V} \right)^{0,4} v_s^{0,4} N^{0,5}$$

For lab fermentors

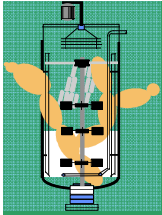
$$K_L a \propto \left(\frac{P_g}{V} \right)^\alpha v_s^\beta N^{0,5}$$

generally

α
0,3 — 0,95

β
0,50 — 67

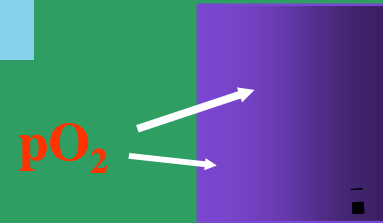
scale dependent constants,



Aeration 3

$$\frac{dC}{dt} = K_L a (C^* - C) - xQ$$

In aerated/agitated reactor



On what and how depends C^* ?

On what and how depends $K_L a$?

$$K_L a \propto \left(\frac{P_g}{V} \right)^\alpha v_s^\beta N^{0,5}$$



$$a = H_0 \frac{6}{d_b}$$

